

---

**SOCIETY OF ACTUARIES**  
**Enterprise Risk Management – General Insurance Extension**

# Exam ERM-GI

**Date:** Friday, May 1, 2015  
**Time:** 8:30 a.m. – 12:45 p.m.

---

## INSTRUCTIONS TO CANDIDATES

### General Instructions

1. This examination has a total of 80 points.

This exam consists of 9 questions, numbered 1 through 9.

The points for each question are indicated at the beginning of the question. Questions 8 and 9 pertain to the extension readings and/or the Case Study, which is enclosed inside the front cover of this exam booklet.

2. Failure to stop writing after time is called will result in the disqualification of your answers or further disciplinary action.
3. While every attempt is made to avoid defective questions, sometimes they do occur. If you believe a question is defective, the supervisor or proctor cannot give you any guidance beyond the instructions on the exam booklet.

### Written-Answer Instructions

1. Write your candidate number at the top of each sheet. Your name must not appear.
2. Write on only one side of a sheet. Start each question on a fresh sheet. On each sheet, write the number of the question that you are answering. Do not answer more than one question on a single sheet.
3. The answer should be confined to the question as set.
4. When you are asked to calculate, show all your work including any applicable formulas.
5. When you finish, insert all your written-answer sheets into the Essay Answer Envelope. Be sure to hand in all your answer sheets because they cannot be accepted later. Seal the envelope and write your candidate number in the space provided on the outside of the envelope. Check the appropriate box to indicate Exam ERM-GI.
6. Be sure your written-answer envelope is signed because if it is not, your examination will not be graded.

Tournez le cahier d'examen pour la version française.



## **CASE STUDY INSTRUCTIONS**

**The case study will be used as a basis for some examination questions. Be sure to answer the question asked by referring to the case study. For example, when asked for advantages of a particular plan design to a company referenced in the case study, your response should be limited to that company. Other advantages should not be listed, as they are extraneous to the question and will result in no additional credit. Further, if they conflict with the applicable advantages, no credit will be given.**



**\*\*BEGINNING OF EXAMINATION\*\***

- 1.** (5 points) You are an actuary at Myers Insurance Company, which offers a wide range of property and casualty insurance products. You have determined that the company's concentration risk limits have been breached. You have recommended to management that they explore the option of transferring some of the risk to a third party.

Management is only willing to consider reinsurance that attaches at the risk limit.

- (a) (1 point) Explain how reinsurance could be used to address Myers' breach in risk limits.

Myers has the option of entering into one of the following two reinsurance agreements:

- I. Hayden Re: Surplus reinsurance with \$60 retention and \$240 capacity
- II. Tarpon Re: Excess of loss reinsurance with priority \$50 and \$100 capacity

Hayden Re has an AA credit rating, and Tarpon Re has an A- credit rating.

- (b) (0.5 points) Compare and contrast surplus reinsurance with excess of loss reinsurance.
- (c) (1.5 points) Calculate Myers' retained claim for each of the following scenarios. Show your work.

Myers Retained Claims Under Reinsurance Agreements

| Scenario | Sum Insured | Size of Claim | Retained Claim Agreement I | Retained Claim Agreement II |
|----------|-------------|---------------|----------------------------|-----------------------------|
| A        | \$100       | \$20          |                            |                             |
| B        | \$300       | \$200         |                            |                             |

You have determined that entering into either one of these agreements will bring Myers back within its concentration risk limits.

- (d) (2 points) Outline the considerations that would factor into making a recommendation between the two reinsurance options.

2. (8 points) Calusa Insurance Solutions is a large multi-line insurance company that offers life, health, property and casualty, and pension products. Calusa is undergoing changes within each insurance division, and management is concerned with the risks resulting from these changes.

- (a) (2 points) Calusa's Life Insurance division specializes in term life insurance. Currently all of Calusa's term products use the same underwriting process. The underwriting process is very thorough, requiring a full medical examination.

Calusa is considering the addition of a "simplified issue" term product. The simplified issue product would only require an applicant to answer a few questions regarding medical history, with no verification of the answers required. If an applicant answers the questions in an acceptable manner, the policy is issued. All approved applicants of the same age and gender receive the same premium rates.

- (i) Describe the main risk that would be introduced by the simplified underwriting product.
- (ii) Propose strategies to manage the risk identified.

- (b) (2 points) Calusa's Pension division offers a pension product to small and mid-size companies with defined benefit pension plans. The current pension product provides guaranteed immediate annuities to pension plan participants at their retirement, with level monthly payments for life. Calusa is considering the addition of a new pension product with a Cost of Living Adjustment (COLA) feature.

- (i) Describe the main risk that would be introduced by the COLA feature.
- (ii) Propose strategies to manage the risk identified.

- (c) (2 points) Calusa's Property and Casualty (P&C) division has recently experienced employee turnover in the claims department, resulting in experienced employees being replaced by new hires. In addition, Calusa hires temporary employees to assist with data entry during high volume periods.

- (i) Describe the main risk associated with Calusa's personnel practices.
- (ii) Propose strategies to manage the risk identified.

## 2. Continued

- (d) (2 points) Calusa's Health division is in the process of implementing a new internet-based claims administration system. The new system would result in Calusa data being hosted on third party servers and allow Calusa employees to access this data remotely.
- (i) Describe a significant risk associated with the new claims administration system.
  - (ii) Propose strategies to manage the risk identified.

- 3.** (12 points) In 2012, Dr. Dan opened an animal hospital in a small but growing town near a medium-sized city. Dr. Dan is the hospital's only veterinarian and is not paid a salary. He started the business with a bank loan and is not competent with cash management of the business. The hospital has not yet earned a profit but is expected to become profitable in 2015. Dr. Dan expects he could sell the hospital for an amount equal to its outstanding debt.

Dr. Dan enjoys the freedom of being his own boss but struggles with the challenges of managing a business. For example, he has had trouble collecting money his clients owe him, and he acknowledges that he does not manage his employees effectively.

Dr. Dan has hired you as a personal advisor to conduct an independent analysis of the following three strategic options:

- I. Continue his current business with no change.
- II. Sell his hospital and become a staff veterinarian at another animal hospital.
- III. Sell his hospital and take a loan to buy a franchise of a MegaPet animal hospital in the nearby city. MegaPet is a chain of animal hospitals housed exclusively inside a national chain of large pet stores.

You are provided the following simplified financial projections in thousands:

| Calendar Year               | Option I  |           |           | Option II |          |          | Option III |           |           |
|-----------------------------|-----------|-----------|-----------|-----------|----------|----------|------------|-----------|-----------|
|                             | 2015      | 2016      | 2017      | 2015      | 2016     | 2017     | 2015       | 2016      | 2017      |
| Gross Revenue               | 190       | 290       | 388       | 100       | 104      | 108      | 250        | 600       | 900       |
| Client accounts written off | <u>30</u> | <u>35</u> | <u>40</u> | <u>0</u>  | <u>0</u> | <u>0</u> | <u>5</u>   | <u>10</u> | <u>20</u> |
| Net Revenue                 | 160       | 255       | 348       | 100       | 104      | 108      | 245        | 590       | 880       |
| Debt service                | 18        | 18        | 18        | 0         | 0        | 0        | 20         | 25        | 30        |
| Fees to MegaPet             | 0         | 0         | 0         | 0         | 0        | 0        | 50         | 100       | 200       |
| Professional liability ins. | 2         | 2         | 4         | 0         | 0        | 0        | 2          | 4         | 6         |
| Salaries/wages              | 75        | 125       | 220       | 0         | 0        | 0        | 125        | 250       | 375       |
| Employee benefits           | 0         | 0         | 10        | 0         | 0        | 0        | 19         | 38        | 56        |
| Other Expenses              | <u>35</u> | <u>45</u> | <u>55</u> | <u>0</u>  | <u>0</u> | <u>0</u> | <u>45</u>  | <u>65</u> | <u>85</u> |
| Total Expenses              | 130       | 190       | 307       | 0         | 0        | 0        | 261        | 482       | 752       |
| Net Income                  | 30        | 65        | 41        | 100       | 104      | 108      | (16)       | 109       | 128       |

You can ignore taxes in your analysis.



### 3. Continued

You are also provided with the following information regarding the three options:

Option I:

- Projections provide for adding one veterinarian to staff in 2017
- Employee benefits for 2017 are for the second veterinarian only
- Salaries/wages are for support staff in 2015 – 2017 plus the second veterinarian in 2017
- Dr. Dan does not pay himself a salary but receives the hospital's net income each year

Option II:

- The net income represents the salary Dr. Dan receives as an employee

Option III:

- Projections provide for adding one veterinarian in 2016 and a second in 2017
- Dr. Dan does not receive a salary but receives the net income each year
- In addition to branding, MegaPet will:
  - Supply a state-of-the-art hospital administration computer system
  - Monitor the management reports generated by the administration system and communicate with Dr. Dan about potential problems
  - Provide standard policies and procedures that all their hospitals must follow (including requiring clients to pay for the cost of veterinary services at the time of service)
  - Supply training for all employees
  - Purchase most supplies in bulk and handle payments to suppliers
  - Require that employee benefits be made available to all hospital employees

- (a) (3 points) Describe the following risks to Dr. Dan as they apply to Option I:
- (i) Liquidity Risk
  - (ii) Counterparty Risk
  - (iii) Operational Risk
  - (iv) Professional Liability Risk (Legal obligations arising out of a professional's errors, negligent acts, or omissions during the course of the practice of his or her craft)
- (b) (2 points) Explain how the risks described in (a) change if Dr. Dan elects to pursue Option II.

*Question 3 continued on next page*

### 3. Continued

- (c) (2 points) Explain how the risks described in (a) change if Dr. Dan elects to pursue Option III.

As his advisor, you suggest that objective analysis of the risks should not be Dr. Dan's only consideration.

- (d) (2.5 points)
- (i) Explain why, in the strategic risk management field, scenario analysis is adopted as a qualitative analytical tool, rather than as a quantitative tool.
  - (ii) Identify three qualitative factors that could influence Dr. Dan's choice among the three options.
- (e) (2.5 points) You do not intend to make a firm recommendation to Dr. Dan regarding his options; instead, you will offer guidance to help Dr. Dan make the decision that is best for him.

Outline the guidance you will offer Dr. Dan as he chooses among the three options.

4. (5 points) Cypress is a financial services company evaluating the economic performance of two of its operating units. You are provided the following:

|                               | Unit A  | Unit B  |
|-------------------------------|---------|---------|
| Net Income                    | 26.1    | 30.8    |
| Assets                        | 1,000.0 | 1,100.0 |
| Required Economic Capital     | 220.0   | 230.0   |
| Available Economic Capital    | 225.0   | 275.0   |
| Risk Adjustment to Net Income | 9.5     | 13.2    |

Values are reported in \$ millions.

- (a) (2 points) Calculate the following measures of return for each unit:
- (i) ROA
  - (ii) ROE
  - (iii) RAROC
  - (iv) RORAC
  - (v) RARORAC
- Show your work.
- (b) (1 point) Explain the benefits of using risk-adjusted return measures as compared to traditional measures.
- (c) (2 points) The CFO of Cypress concludes from your calculations that unit B is underperforming based on the RAROC measure.
- (i) Explain why the CFO may be most focused on the RAROC measure.
  - (ii) Provide arguments to counter the CFO's conclusion that unit B is underperforming.

5. (10 points) Acme Corporation, a high tech firm, and Elliott, Inc., a traditional manufacturer of high-end furniture, each has outstanding zero coupon debt of \$100 million maturing in three years. This is the only debt outstanding for each company.

You intend to use the Merton model to evaluate the debt.

The companies currently have the following characteristics:

|         | <b>Assets</b> | <b>Expected Growth Rate</b> | <b>Volatility</b> |
|---------|---------------|-----------------------------|-------------------|
| Acme    | \$175M        | 0.12                        | 0.36              |
| Elliott | \$250M        | 0.04                        | 0.29              |

- (a) (2.5 points)
- (i) Explain how the payoffs to Acme's bondholders and stockholders can be viewed in terms of puts and calls.
  - (ii) Graph the payoffs to Acme's stockholders as a function of the potential asset values at the end of year three. Label your graph.
  - (iii) Graph the payoffs to Acme's bondholders as a function of the potential asset values at the end of year three. Label your graph.
- (b) (2 points) Show that the probability of default at the end of year three using the Merton model is:
- (i) 12.2% for Acme
  - (ii) 3.5% for Elliott.
- (c) (0.5 points) First, assume that there is no dependence between the two companies.

Calculate the probability that both companies will default at the end of year three. Show your work.

## 5. Continued

- (d) (5 points) Next, assume that the asset values at time 3 of the two companies are linked by a Clayton Copula with parameter  $\alpha = 2$ .

The Clayton Copula has a generalized function:

$$C_{\alpha}(F(x_1), F(x_2), \dots, F(x_N)) = \left[ \sum_{n=1}^N (F(x_n))^{-\alpha} - N + 1 \right]^{-\frac{1}{\alpha}}$$

- (i) Show that the probability that both companies will default at the end of year three using the Clayton Copula is 3.4%.
- (ii) Explain why the maximum possible value for the probability that both companies will default at the end of year three is 3.5%.
- (iii) State with reasons whether the Clayton Copula with parameter  $\alpha = 2$  is an appropriate model for the joint probability functions for the two distributions in this case.

6. (11 points) Gaia Insurance is a life insurer that has historically sold life insurance and annuity contracts. Gaia has been measuring its economic capital for this business using a parametric VaR of its profits and losses (P&L). VaR is measured using a quarterly horizon with a 95% confidence level. The profits are assumed to be normally distributed with a quarterly mean profit of \$5 million and a standard deviation of \$8 million.

You have been asked to review alternative calculation methods for VaR.

The following table provides the worst ten ordered quarterly losses for Gaia over the last 100 quarters:

|                        |      |      |      |     |     |     |     |     |     |     |
|------------------------|------|------|------|-----|-----|-----|-----|-----|-----|-----|
| Losses<br>(\$millions) | 13.5 | 11.3 | 10.1 | 9.0 | 8.2 | 7.4 | 6.8 | 6.2 | 5.7 | 5.3 |
|------------------------|------|------|------|-----|-----|-----|-----|-----|-----|-----|

- (a) (1.5 points) Calculate the following risk metrics for Gaia's life and annuity block at a 95% confidence level over a quarterly horizon:

- (i) Parametric VaR
- (ii) Empirical VaR

Show your work.

- (b) (2 points) You recall the following standard error formulas:

$$SE(\hat{q}) = \sqrt{\frac{c(1-c)}{Tf(q)^2}}$$

$$SE(\hat{\sigma}) = \sigma \sqrt{\frac{1}{2T}}$$

Calculate a 95% confidence interval for each of the following risk metrics with respect to a sample of 100 observations that have an underlying Normal distribution:

- (i) 95% Parametric VaR
- (ii) 95% Empirical VaR

Show your work.

- (c) (1.5 points) Assess whether the parametric or empirical VaR is the better approach for Gaia's life and annuity block. Explain your conclusions using your analysis in (a) and (b).

## 6. Continued

Gaia recently acquired Kismah General, a property insurer.

You have constructed a distribution of annual P&L (in \$millions) per \$100 million earned premiums based on industry data that you will use to assess the risk exposure of Kismah General. The data has a mean profit of \$30 million, a standard deviation of \$30 million and the following annual loss tail:

| Percentile | 1 <sup>st</sup> | 2 <sup>nd</sup> | 3 <sup>rd</sup> | 4 <sup>th</sup> | 5 <sup>th</sup> | 6 <sup>th</sup> | 7 <sup>th</sup> | 8 <sup>th</sup> | 9 <sup>th</sup> | 10 <sup>th</sup> |
|------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|------------------|
| Losses     | 145             | 111             | 86              | 82              | 41              | 21              | 16              | 13              | 11              | 8                |

(d) (1 point) Calculate the following risk metrics for Kismah General over a one-year horizon and at a 98% confidence level:

- (i) Parametric VaR, assuming losses are normally distributed
- (ii) Empirical VaR

Show your work.

(e) (2 points)

(i) Plot the losses predicted by assuming a Normal  $(30, 30^2)$  distribution for the P&L of the Kismah General insurance block against the historical values at the following percentiles:

- 1. 90<sup>th</sup>
- 2. 95<sup>th</sup>
- 3. 99<sup>th</sup>

(ii) Interpret the results.

For the Kismah General insurance block, you also investigate the use of extreme value theory (EVT), fitting a two-parameter generalized Pareto distribution (GPD) to the tail of the historic loss data. The GPD has the following cumulative distribution function:

$$F(x) = 1 - \left( 1 + \xi \frac{x-u}{\beta} \right)^{-\frac{1}{\xi}}$$

*Question 6 continued on next page*

## 6. Continued

Using a loss of \$41 million as the threshold, beyond which 5% of the dataset remains, you determine that the maximum likelihood estimate of the shape parameter is 0.5 and of the scale parameter is \$100.

Using the GPD for the tail losses, the estimated VaR at the  $c^{\text{th}}$  level of confidence is:

$$\widehat{\text{VaR}} = u + \left( \hat{\beta} / \hat{\xi} \right) \left\{ \left[ (N / N_u)(1-c) \right]^{-\hat{\xi}} - 1 \right\}$$

- (f) (1 point) Calculate the 98<sup>th</sup> percent quantile estimator of VaR using your fitted Generalized Pareto model. Show your work.
- (g) (2 points) Recommend the most appropriate method for estimating VaR from those computed in (d) and (f) to use for the Kismah General insurance block. Justify your choice with reference to specific results from your analysis.



**THIS PAGE INTENTIONALLY LEFT BLANK**

7. (9 points) You are an actuary at Bunche Mutual. Bunche's models are developed and maintained by the pricing actuaries. These models are then provided by the various pricing actuary teams to the corporate risk actuaries and converted for internal capital purposes. While the pricing actuaries have a strong sense of ownership over their models, they are not knowledgeable about the internal capital model results.

The corporate risk actuaries set capital using 90% CTE. Some of the assumptions in the Economic Capital (EC) model have not been changed since the model was developed five years ago.

You have been asked to validate the EC model based on the following three principles:

- I. Model design and build need to be consistent with the model's intended purpose
  - II. Ensure appropriateness of established model governance
  - III. Validate the model components
- (a) (1.5 points) Describe potential areas of concern with model governance (Principle II) at Bunche.
- (b) (2 points) You are validating the model parameters for the following risks:
- (i) Pandemic Risk
  - (ii) Operational Risk
  - (iii) Expense Risk

Identify an appropriate estimation method for parameterizing each of the risks listed above. Explain your response.

## 7. Continued

Your manager tells you that the only assumptions you need to validate are mortality and lapse.

- (c) (2.5 points) The mortality assumption currently used in the model was provided by a consultant five years ago and has not been updated since. There have been changes to the product designs and mix of business in the last five years.
  - (i) Identify key considerations that should be taken into account in updating Bunche's mortality assumption.
  - (ii) Explain how to apply each of Principles I, II, and III to the mortality updating process.
- (d) (3 points) Outline the process you would follow to determine if your manager's focus on validating only the mortality and lapse assumptions in the EC model is appropriate.

*Questions 8 and 9 pertain to the Case Study and/or extension readings.  
Each question should be answered independently.*

**8.** (12 points) Senior management at Pryde has noticed the apparent success of its industry competitors in using the internet for direct marketing of personal lines insurance. Given Pryde's past failures with new production sources and customer segments, you have been asked to look very carefully at the viability of such a direct marketing strategy for Pryde's personal lines.

(a) (1 point) Explain Panning's concept of "franchise value" to senior management, as it applies to direct marketing of personal lines insurance.

To illustrate the hidden franchise value of direct-marketed personal lines insurance to senior management, you develop a simplified firm model such that:

- Premiums are received and expenses are incurred on January 1
- Expected losses are paid at the end of the year
- Surplus is maintained at the same level throughout the projected period (by dividending out profits or receiving capital infusion on an annual basis)
- Expenses and losses are the same every year
- The yield curve is flat
- The current risk-free rate is  $y = 2\%$
- The client retention rate is 90%
- Taxes are ignored
- Calculations are as of January 1 after premiums are received and expenses paid

The pricing policy of the simplified firm is to set premiums to earn a specified target return on surplus.

(b) (4 points) Assuming for the simplified firm that Surplus is 100, Losses are 150, Expenses are 50, and the target return is  $k = 12\%$ :

- (i) Calculate the premium level that achieves the firm's target return on surplus.
- (ii) Calculate the current economic value of the firm.
- (iii) Calculate the franchise value of the firm.
- (iv) Calculate the total economic value of the firm.

Show your work.

## 8. Continued

- (c) (3 points) The assets backing the simplified firm have a duration of one year, matching the maturity of the expected liabilities.

You have been given the following formula for the duration of the franchise value under Panning's framework:

$$D = \frac{(a-b+1)}{(1+y)(a+by-y)} + \frac{1}{(1+y-r)}$$

Assume the firm uses a fixed 12% pricing strategy independent of the risk free rate.

Determine the duration of the following values:

- (i) Franchise value
- (ii) Current economic value
- (iii) Total economic value

Show your work.

- (d) (1 point) Explain why the duration of the firm's franchise value in (c)(i) above is relatively high as compared to the asset duration.
- (e) (3 points) Pryde's current pricing strategy is to achieve a 10% risk premium over the risk free rate, as opposed to the fixed 12% pricing strategy used above.

Pryde's ALM strategy is to manage its overall asset duration to within 0.5 years of a target duration of 4.5 years.

- (i) Apply Pryde's current pricing strategy to the simplified firm to estimate the duration of the total economic value. Show your work.
- (ii) Explain why linking the pricing strategy to the risk premium reduces the duration of the firm's total economic value.

**Questions 8 and 9 pertain to the Case Study and/or extension readings.  
Each question should be answered independently.**

- 9.** (8 points) You have been asked to evaluate Pryde's surplus position.
- (a) (1 point) Calculate the following ratios for Pryde as of year-end 2014:
- (i) Premium to statutory surplus
  - (ii) Statutory surplus to statutory reserves
  - (iii) Statutory surplus to required economic capital
- Show your work.
- (b) (1 point) Explain why each of these ratios might be an inappropriate way to determine company financial strength.
- (c) (1 point) Propose an alternative method to measure capital needs other than the computation of Economic Capital.

## 9. Continued

- (d) (3.5 points) Pryde's stochastic simulation of 10,000 scenarios produced the following tails of the cumulative probability distributions (CPD) of claims, in millions of dollars.

| Claims CPDs          |                          |                          |
|----------------------|--------------------------|--------------------------|
| Cumulative Frequency | Pryde (All LOB combined) | Workers Compensation LOB |
| 0.984                | \$750                    | \$250                    |
| 0.986                | 775                      | 264                      |
| 0.988                | 810                      | 290                      |
| 0.990                | 822                      | 300                      |
| 0.992                | 825                      | 310                      |
| 0.994                | 902                      | 360                      |
| 0.996                | 950                      | 410                      |
| 0.998                | 1,730                    | 460                      |

- (i) Calculate VaR 99.0 for Pryde in total and for the Workers Compensation line of business (LOB). Show your work.
- (ii) Estimate TVaR 99.0 for Pryde in total and for the Workers Compensation line of business (LOB). Show your work.
- (iii) Explain the limitations of estimating TVaR using these CPDs.
- (e) (1.5 points) Pryde decides to get a stop loss reinsurance quote on the Workers Compensation LOB with a break-even retention. The reinsurer quotes a premium of \$35 million for this coverage. Pryde's internal modeling estimates that the premium for this stop loss coverage should be \$20 million.
- (i) Describe the relationship between these premiums and the desired profitability of the LOB.
- (ii) Explain possible reasons for the difference in the two values.

**\*\*END OF EXAMINATION\*\***

**USE THIS PAGE FOR YOUR SCRATCH WORK**